

DINÁMICA I

LEYES DE NEWTON

4) $m = 2300 \text{ t}$
 $\vec{F}_m = 3 \cdot 10^7 \text{ N}$

$P = 2300 \cdot 1000 \cdot 9.81 = 2.3 \cdot 10^6 \cdot 9.81$
 $= 22.56 \cdot 10^6 ;$

b) $F_T = F_m - P$

$F_m = 30 \cdot 10^6 - 22.56 \cdot 10^6 = 7.437 \cdot 10^6 \text{ N}$

c) $\vec{F} = m \cdot a = 2.3 \cdot 10^6 \text{ e} ;$

$7.437 \cdot 10^6 = 2.3 \cdot 10^6 \cdot e ;$

$e = 3.2 \text{ m/s}^2$

③ 150 N durante 0.1 s
 below 450 s

$\vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t} ; \quad \Delta \vec{v} = \frac{F \cdot \Delta t}{m} = \frac{150 \cdot 0.1}{0.4} =$
 $= 37.5 \text{ m/s}$

⑦ 120 km/h = 33.33 m/s
 15 millimeters = 0.015 s
 0.05 s

$\vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t} ; \quad \vec{F} = \frac{0.058 \cdot 33.33}{0.015} = 128.88 \text{ N}$

b) $\vec{a}_m = \frac{\vec{v}}{\Delta t} = \frac{33.33}{0.015} = 2222.22 \text{ m/s}^2$

EJEMPLOS RESUELTOS

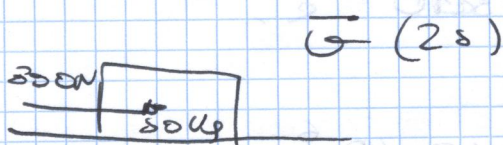
10-12

- ⑩ 1200 kg a 108 km/h (30 m/s)
6 s en frenar.

F frenos:

$$\vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t} = \frac{1200 \cdot (0 - 30)}{6} = -6000 \text{ N} //$$

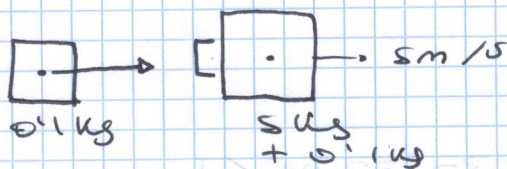
- ⑪ 300 N 50 kg



$$F = \frac{m \cdot \Delta \vec{v}}{t}; \quad 300 = \frac{50 \cdot \Delta \vec{v}}{2};$$

$$\Delta \vec{v} = 12 \text{ m/s} //$$

⑫



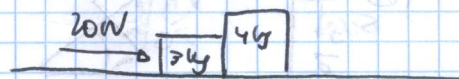
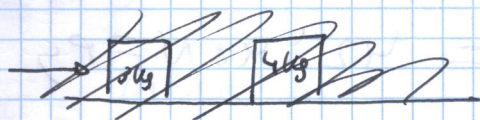
100 s

$$\vec{p} = m \cdot \vec{v} \quad (p_{\text{total}})_{\text{inicial}} = (p_{\text{total}})_{\text{final}};$$

$$0.1 \cdot \vec{v}_1 = 5.1 \cdot 5 \text{ m/s};$$

$$\vec{v}_1 = 285 \text{ m/s} //$$

(13)



aceleración del conjunto.
 $a = \frac{0.6}{0.5}$

$$\vec{F} = m \cdot a = m \cdot \vec{a}$$

$$\vec{F} = \frac{m \cdot \vec{a}}{t}$$

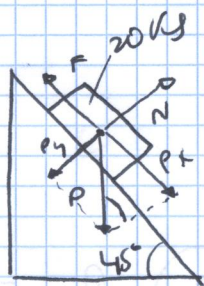
aceleración del conjunto:

$$\vec{F} = m(m_1 + m_2) \cdot a;$$

$$20 = 7 \cdot a; \quad a = 2.86 \text{ m/s}^2$$

En la misma aceleración de A a B y de B a A.

(14)



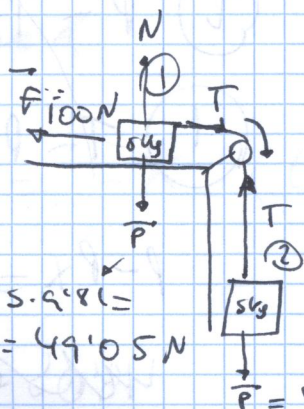
$$P = 20 \text{ kg} \cdot 9.81 = 196.2$$

$$P_x = \sin 45^\circ \cdot 20 = 138.73$$

$$P_y = \cos 45^\circ \cdot 20 = 141.4 \text{ N} \cdot 9.81 = 138.73$$

$$F = 138.73$$

(15)



④

$$\vec{F} = m \cdot a;$$

$$\textcircled{1} \quad 100 - T = 5 \cdot a;$$

$$\textcircled{2} \quad 49.05 - T = 5 \cdot a$$

$$\begin{aligned} -100 + T &= -5 \cdot a \\ 49.05 - T &= 5 \cdot a \\ \hline -50.95 &= -10 \cdot a \\ a &= 5.095 \end{aligned}$$

$$5 \cdot 9.81 = 49.05 \text{ N}$$

$$\vec{P} = 49.05 \text{ N}$$

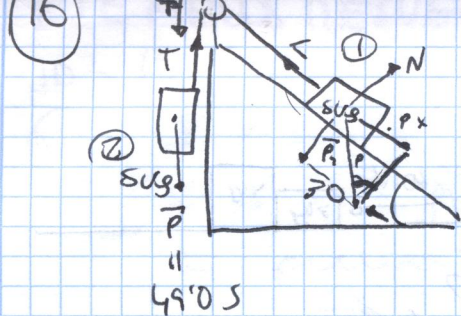
$$74.52 - 49.05 = 5 \cdot a;$$

$$a = 5.095 \text{ m/s}^2$$

$$\begin{aligned} T - P &= ma \\ P - T &= ma \end{aligned}$$

$$\frac{T - P}{P - T} = 1;$$

$$\frac{T - 49.05}{100 - T} = 1;$$



$$P_x = 8000 \cdot 49'05 = 24'525 \text{ N}$$

$$P_y = 8000 \cdot 49'05 = 42'48 \text{ N}$$

$$N = 42'48 \text{ N} = P_y$$

acceleration?

$$\begin{aligned} \textcircled{1} & P_x - T = m \cdot a \\ \textcircled{2} & P - T = m \cdot a \end{aligned}$$

$$\begin{aligned} P_x - T &= m \cdot a \\ T - P &= m \cdot a \end{aligned}$$

$$\begin{aligned} -T + P_x &= m \cdot a \\ T - P &= m \cdot a \end{aligned}$$

$$\begin{aligned} -P_x + T &= -m \cdot a \\ P - T &= m \cdot a \\ \hline -P_x + T &= -m \cdot a \\ P - T &= m \cdot a \\ \hline -P_x + P &= -2m \cdot a \\ \hline P - P_x &= 2m \cdot a \end{aligned}$$

$$24'525 - 42'48 = 10a$$

$$a = -2'45$$

$$\textcircled{2} P - T = m \cdot a$$

$$\textcircled{1}$$

$$\begin{aligned} P_x - T &= m \cdot a \\ P - T &= m \cdot a \\ \hline P_x - T &= P - T \end{aligned}$$

$$\begin{aligned} -P_x + T &= -m \cdot a \\ P - T &= m \cdot a \\ \hline -24'525 + 42'48 &= 10a \end{aligned}$$

$$\textcircled{2} P - T = m \cdot a$$

$$\textcircled{1} T - P_x = m \cdot a$$

$$P - P_x = 2m \cdot a$$

$$42'48 - 24'525 = 2m \cdot a$$

$$mg - mg \cos \alpha = 2ma$$

$$mg(1 - \cos \alpha) = 2ma$$

$$a = \frac{(1 - \cos \alpha)g}{2}$$

$$\vec{F} = m \cdot \vec{g}$$

$$p = m \cdot \Delta \vec{v}$$

$$\vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t}$$

$$p' = m \cdot \vec{v}$$

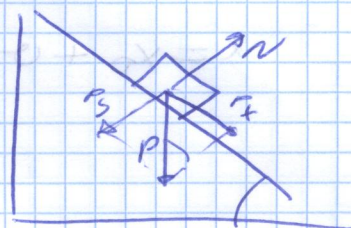
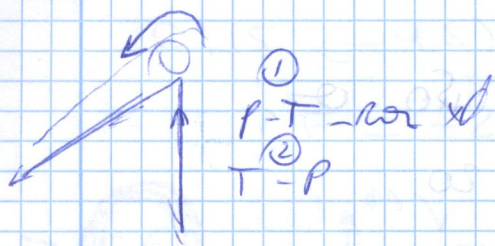
$$m \cdot \vec{v} = \vec{F} \cdot \Delta t$$

$$\vec{F} = \frac{p}{\Delta t}$$

$$\vec{p} = m \cdot \vec{v}$$

Força opõe al movimento

$$F_{roz} = N \cdot \mu$$



$$P_x = P \cdot \sin \alpha$$

$$P_y = P \cdot \cos \alpha$$

gravitação
unil

$$F_g = G \cdot \frac{m_1 \cdot m_2}{d^2}$$

$$G = 6.67 \cdot 10^{-11}$$

$$\vec{F} = k \cdot \frac{Q_1 \cdot Q_2}{d^2} \cdot \vec{u}$$

hook

$$F = -K \cdot (l - l_0)$$

↑
x

dúda:

como se
calcula a
obj em baixos
plano inclinados

$$\Sigma \vec{F} = m \cdot \vec{a};$$

$$\Sigma \vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t};$$

$$\vec{v} = \frac{\vec{p}}{\Delta t};$$

$$\Delta \vec{p} = m \cdot \Delta \vec{v};$$

$$m \cdot \Delta \vec{v} = \Delta t \cdot \Sigma \vec{F};$$

$$\vec{p}_1 = \vec{p}_2$$

$$m_1 \cdot v_1 = m_2 \cdot v_2$$

$$I = m \cdot \vec{v}$$

$$\frac{200N}{\boxed{5s}} \quad ss;$$

mrh

$$\vec{p} = \Delta t \cdot \Sigma F = 5 \cdot 200 = 1000 N$$

$$x = x_0 + v_0 \cdot t; \quad 1000 = 50 \cdot v;$$

$$v = 20$$

~~$$1000 = 15 \cdot v$$~~

$$x = 0 + 20 \cdot 5 = 100 m$$

(23)

$$15N \rightarrow \boxed{104}$$

$$v_0 = 0 m/s \quad t = 0 s$$

$$v_f = 30 m/s \quad t = ?$$

$$p_{initial} = p_{final}$$

$$10 \cdot 30 = \Delta t \cdot 15;$$

$$\Delta t = \frac{300}{15} = 20 s //$$

(25)

$$m \cdot \vec{v} = \Delta t \cdot F$$

$$F = \frac{m \cdot \vec{v}}{t}$$

$$150 \text{ g} = 0.15 \text{ kg}$$

$$45 \text{ m/s}$$

detenido en 0.3 s

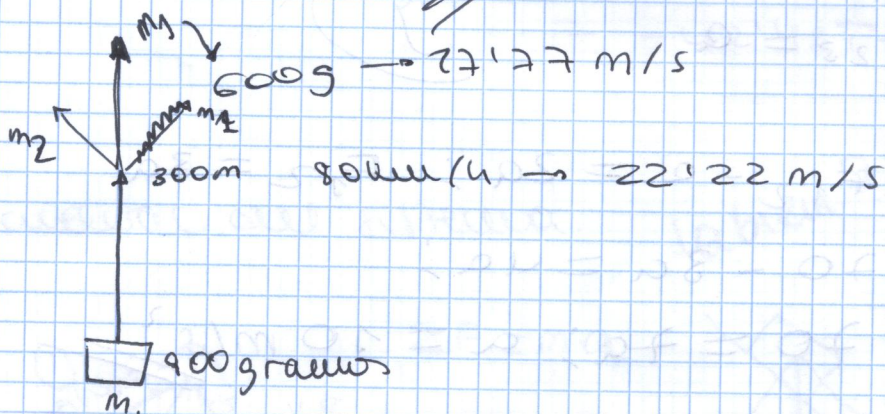
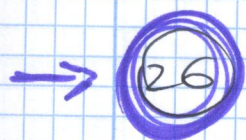
$$\Delta \vec{v} = 0.3 \text{ s}$$

$$\Delta \vec{v} = -45 \text{ m/s}$$

$$v_2 - v_1$$

$$0.15 \cdot (-45) = 0.3 \cdot F$$

$$F = -22.5 \text{ N}$$



$$(\vec{P}_{\text{total}}^{\text{initial}}) = (\vec{P}_{\text{total}}^{\text{final}});$$

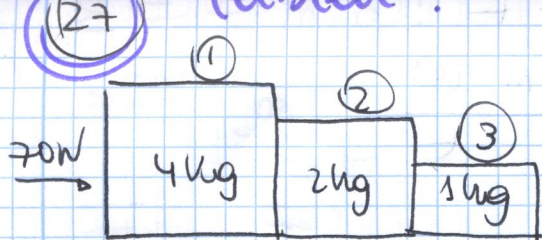
~~(1/2)~~

$$(m_1 + m_2) \cdot 22.22 = m_1 \cdot 27.77 + m_2 \cdot v_2;$$

$$0.900 \cdot 22.22 = 0.600 \cdot 27.77 + 0.300 \cdot v_2;$$

$$v_2 = 11.11 \text{ m/s}$$

¿hacia donde va?
ángulo?



acceleration?

$$\Sigma F = m \cdot a$$

$$\Sigma F = \frac{m \cdot v}{t}$$

$$\textcircled{1} F - F_{12} = m_1 \cdot a$$

$$\textcircled{2} F_{12} - F_{23} = m_2 \cdot a$$

$$\textcircled{3} F_{23} = m_3 \cdot a$$

$$1) 70 - F_{12} = 4 \cdot a$$

$$2) F_{12} - F_{23} = 2 \cdot a$$

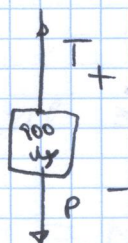
$$3) F_{23} = a$$

$$2) F_{12} - a = 2a; F_{12} = 3a$$

$$1) 70 - 3a = 4a;$$

$$70 = 7a; a = 10 \text{ m/s}^2$$

(28)



$$T_{\max} = 12000 \text{ N};$$

$$P = 8829 \text{ N}$$

a) máxima aceleração?

$$\Sigma F = m \cdot a;$$

$$T - P = m \cdot a;$$

$$12000 - 8829 = 700 \cdot a;$$

$$a = 3.52 \text{ m/s}^2$$

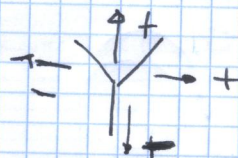
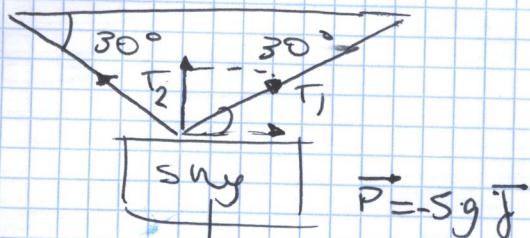
$$b) \Sigma F = m \cdot a$$

$$T - 8829 = 700 \cdot 3.52;$$

$$T = 11079 \text{ N}$$

(29)

What? decomposition tension en composantes?



$$\vec{T}_1 = T \cdot \cos 30^\circ \vec{i} + T \cdot \sin 30^\circ \vec{j}$$

$$\vec{T}_2 = T \cdot \cos 30^\circ \vec{i} + T \cdot \sin 30^\circ \vec{j}$$

$$\Sigma \vec{F} = (\vec{T}_1 + \vec{T}_2) + \vec{P} = 0,$$

$$\vec{T}_1 + \vec{T}_2 = -\vec{P} = 5g \vec{j}$$

$$\vec{T}_1 + \vec{T}_2 = 2T \cdot \sin 30^\circ \vec{j}$$

$$5g \vec{j} = 2T \sin 30^\circ \vec{j}$$

$$T = 5g$$

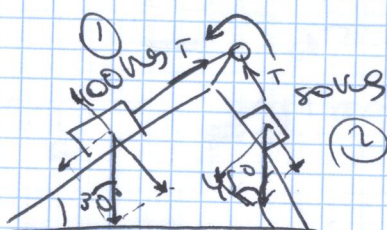
$$\vec{T}_1 = 5g \cdot \cos 30^\circ \vec{i} + 5g \cdot \sin 30^\circ \vec{j} = 42'48 \vec{i} + 24'52 \vec{j}$$

$$\vec{T}_2 = -5g \cdot \cos 30^\circ \vec{i} + 5g \cdot \sin 30^\circ \vec{j} = -42'48 \vec{i} + 24'52 \vec{j}$$

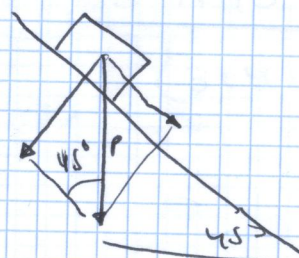
(30)

accélération du système.

labien?



$$\Sigma F = ma$$



(1)

$$\Sigma F = m \cdot a$$

$$P = 100 \cdot 9'81 = 981 \text{ N}$$

$$P_x = 981 \cdot \sin 30^\circ = 490'5 \text{ N}$$

$$P_y = 981 \cdot \cos 30^\circ = 849'57 \text{ N}$$

$$P_x - T = 100 \cdot a$$

$$490'5 - T = 100a$$

(2)

$$P_x = P \cdot \sin 45^\circ = 546'84$$

$$T - P_x = 50a$$

$$T - 546'84 = 50a$$

$$+ 490'5 = 100a$$

$$T - 546'84 = 50a$$

$$143'66 = 150a$$

$$143'66 = 150a$$

$$\vec{F} = m \vec{a}$$

$$\vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t}$$

$$\cancel{m_1 \cdot \vec{v}_1} = (\cancel{p_{initial}}) - (\cancel{p_{final}})$$

$$m_1 \cdot v_1 = m_2 \cdot v_2$$

$$\vec{F} = \frac{\Delta p}{\Delta t}$$

ejemplo resueltos

4) $m_T = 5'98 \cdot 10^{24} \text{ kg}$
 $m_L = 7'35 \cdot 10^{22} \text{ kg}$

$$d_{T-L} = 384000 \text{ km} = 384 \cdot 10^6 \text{ m}$$

$$F_T + F_L = 0;$$

$$F_T = F_L;$$

$$F = G \cdot \frac{m_T \cdot m_L}{d^2} = 6'67 \cdot 10^{-11} \cdot \frac{5'98 \cdot 10^{24} \cdot 7'35 \cdot 10^{22}}{(384 \cdot 10^6)^2} =$$

$$= 11'99 \cdot 10^{20} \text{ N}$$

$$F_T = F_L = G \cdot \frac{m_T}{d^2} = G \cdot \frac{m_L}{d^2};$$

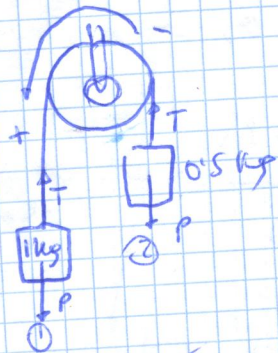
$$\cancel{F_T} \quad G \cdot \frac{m_T}{d^2} = G \cdot \frac{m_L}{d^2}$$

$$d^2 \cdot \cancel{G} \cdot m_T = d^2 \cdot \cancel{G} \cdot m_L$$

$$d^2 \cdot 5'98 \cdot 10^{24} = d^2 \cdot 7'35 \cdot 10^{22}$$

$$5'9065 \cdot 10^{24}$$

5) máquina de Atwood



aceleración sistema = ???

$$\Sigma F = m \cdot a = \frac{m \cdot \vec{a}}{t} = \frac{P}{t}$$

~~$$F_1 = P_1 - T = m \cdot a$$~~

~~$$F_2 = T - P_2 = m \cdot a$$~~

~~$$P_1 - P_2 = m \cdot a$$~~

~~$$9.81 - 4.905 =$$~~

~~$$P_1 - T = m \cdot a$$~~

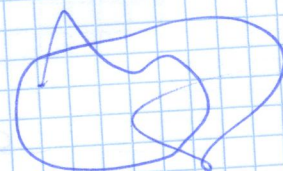
~~$$T - P_2 = 0.5a$$~~

$$9.81 - 4.905 = 0.5a$$

$$a = \frac{4.905}{1.5} = 3.27 \text{ m/s}^2$$

$$T = 0.5a + P_2$$

$$T = 0.5 \cdot 3.27$$



$$g = G \cdot \frac{m_{\text{terra}}}{d^2}$$

$$\textcircled{1} \quad g_{\text{nivel mar}} = G \cdot \frac{M}{(6.370 \cdot 10^6)^2}$$

$$P = m \cdot g = G \cdot \frac{mM}{d^2}$$

$9.81 = g_{\text{nivel mar}} = \text{¿masa Tierra?}$

$$9.81 = 6.67 \cdot 10^{-11} \cdot \frac{M}{(6.370 \cdot 10^6)^2}$$

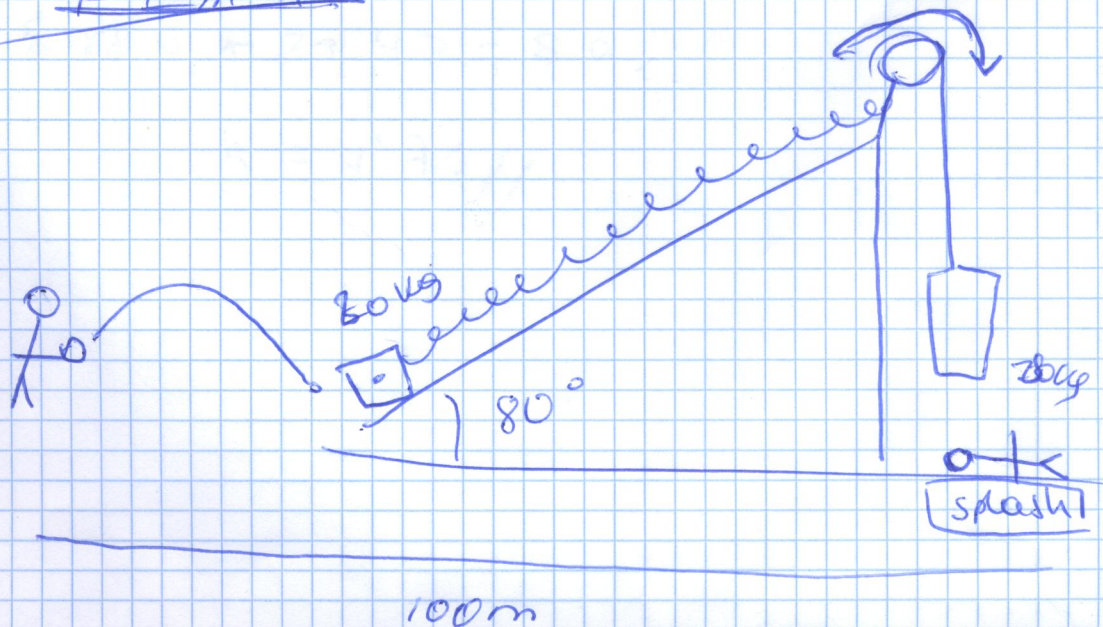
$$M = 5.97 \cdot 10^{24} \text{ kg}$$

persona al nivel del mar: $9.81 - 70 = 686.7 \text{ N}$

$$P = m \cdot g = G \cdot \frac{M - m}{d^2}$$

$$g = 6.67 \cdot 10^{-11} \cdot \frac{5.97 \cdot 10^{24}}{6.370 \cdot 10^6} = 9.8112$$

~~F = m \cdot g~~



ficha

$$F = x \cdot k$$

$$l_f = 40$$

↑

$$(l_f - l_i)$$

$$k = 50 \text{ N/m} =$$

$$= 0.05 \text{ N/cm};$$

$$10 \text{ N}$$

$$x = \frac{F}{k} = \frac{10 \text{ N}}{50 \text{ N/m}}$$

$$x = 0.2 \text{ m} = 20 \text{ cm},$$

elongación

$$l_i = 40 \text{ cm} \rightarrow l_f = 60 \text{ cm}$$

$$x = l_f - l_i$$

$$20 = l_f - 40;$$

$$l_f = 60 \text{ cm}!!$$

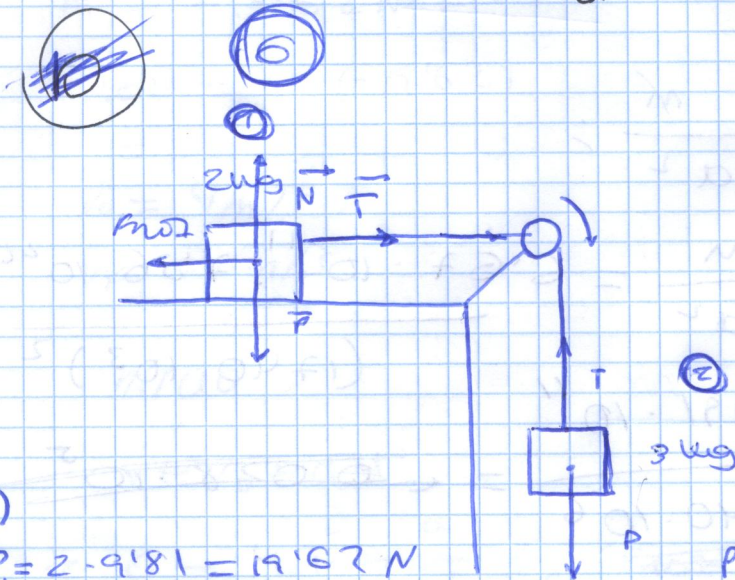
~~$$10 = 0.05 \cdot (l_f - 40)$$~~

~~$$0.05 l_f = 10 - 2$$~~

~~$$l_f = 160$$~~

$$P = m \cdot g = G \cdot \frac{M \cdot m}{d^2}$$

$$g = G \cdot \frac{M}{d^2}$$



1)

$$P_1 = 2 \cdot 9.81 = 19.62 \text{ N}$$

$$N = 19.62 \text{ N}$$

$$P_2 = 3 \cdot 9.81 = 29.43$$

$$F_{\text{roz}} = N \cdot \mu = 19.62 \cdot 0.3 = 5.886$$

1) ~~$T = F_{\text{roz}}$~~

$$\left. \begin{array}{l} T - F_{\text{roz}} = 2a \\ P_2 - T = 3a \end{array} \right\}$$

$$- F_{\text{roz}} + P_2 = 5a$$

$$- 5.886 + 29.43 = 5a$$

$$a = 4.71 //$$

$$(1) \quad g_{UNA} = ?$$

$$m_L = 7'36 \cdot 10^{22} \text{ kg}$$

$$R_L = 1740 \text{ km} = 1740 \cdot 10^3 \text{ m}$$

$$F = m \cdot g$$

$$F = G \cdot \frac{m \cdot m}{d^2}$$

$$g = G \cdot \frac{m}{d^2} = \frac{6'67 \cdot 10^{-11} \cdot 7'36 \cdot 10^{22}}{(1740 \cdot 10^3)^2} =$$

$$= \frac{49'091 \cdot 10^{11}}{1740 \cdot 10^6} = \frac{2'821'322 \cdot 10^5}{1740} =$$

$$= 1'62 \cdot 10^5 \text{ m/s}^2$$

(2) 2 electrons \rightarrow fuerzas repulsivas por tener la misma carga (negativa)

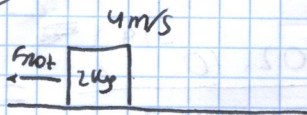
$$F_g = G \cdot \frac{m_1 \cdot m_2}{d^2} = \frac{6'67 \cdot 10^{-11} \cdot (9 \cdot 10^{-31})^2}{d^2} =$$

$$= \frac{5'52 \cdot 10^{-71}}{d^2}$$

$$F_e = 9 \cdot 10^9 \cdot \frac{(-1'6 \cdot 10^{-19})^2}{d^2} = \frac{2'304 \cdot 10^{-28}}{d^2}$$

La eléctrica es mayor

(7)



a deficiu en 5s

$$P = 2 \cdot 9.81 = 19.62 \text{ N};$$

$$N = -19.62 \text{ N} = -P;$$

$$F_{\text{frot}} = \mu \cdot (-19.62)$$

$$v_0 = 4 \text{ m/s};$$

$$v_f = 0 \text{ m/s}$$

m/ua;

$$v = v_0 + a \cdot t$$

$$0 = 4 + a \cdot t; \quad F_{\text{frot}} \cdot t = -4$$

$$-4 = 5 F_{\text{frot}}; \quad F_{\text{frot}} = -\frac{4}{5} = -0.8 \text{ m/s}^2;$$

$$-0.8 = \mu \cdot (-19.62);$$

$$\mu = 0.04$$

$$F_{\text{frot}} = m \cdot a = 2 \cdot (-0.8) = -1.6 \text{ N}$$

(8)

$$l_i = 40 \text{ cm}$$

~~F_{frot}~~~~0.04~~

$$K = 50 \text{ N/m} = 0.5 \text{ N/cm}$$

$$F = K \cdot x;$$

$$x = \frac{F}{K} = \frac{10}{0.5} = 0.2 \text{ m};$$

$$10 = 0.05 \cdot (l_f - 40);$$

$$10 = 0.05 \cdot l_f - 2;$$

$$l_f = \frac{5}{0.05} = 100 \text{ cm}$$

$$l_f - l_i = 0.2;$$

$$l_f - 0.40 = 0.2;$$

$$l_f = 0.6 \text{ m}$$

$$50 \frac{\text{N}}{\text{m}} \cdot \frac{1 \text{ m}}{100 \text{ cm}}$$

1° we have absolute
degree inter-
pt y $e^- \rightarrow$ attraction

$$F = k \cdot \frac{q_1 \cdot q_2}{r^2} = 9 \cdot 10^9 \frac{C^2}{N \cdot m^2}$$

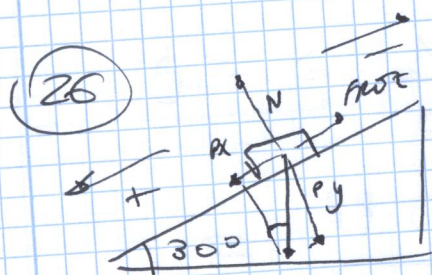
$$F = k_e \cdot \frac{q_1 \cdot q_2}{d^2} = 9 \cdot 10^9 \cdot \frac{(1'602 \cdot 10^{-19})^2}{(s^{-1})^2} =$$

11 ~~5 5 10 13~~ ✓

$9.2 \cdot 10^{-8}$

129 *Impatiens*

$$0.5 \text{ \AA} \cdot \frac{10^{-10} \text{ m}}{1 \text{ \AA}} = 5^{-11}$$



$$a = ?$$

$m = 10 \text{ kg}$ $\mu = 0.2$

$$P = m \cdot g = 98,1 \text{ N}$$

$$P_x = 98'1 \cdot \sin 30^\circ = 49'05 \text{ N}$$

$$p_y = 98'1 \cos 30^\circ = 84'96 \quad \checkmark$$

$$\mathbb{N}:$$

$$f_{\text{rot}} = \mu \cdot N = 0.2 \cdot 84.96 = 16.99 \text{ N}$$

$$\Sigma F = m \cdot a ;$$

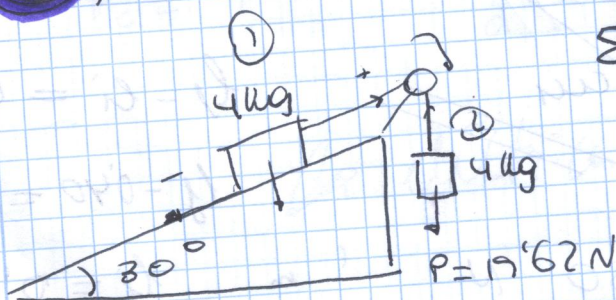
$$P_x - F \cos \theta = m \cdot a;$$

$$49'05 - 16'99 = 10.9'$$

$$a = 3,21 \text{ m/s}^2$$

27 $\mu = ??$

Está em equilíbrio



$$\Sigma F_1 = \Sigma F_2$$

① $P = 39.24 \text{ N}$

$$P_x = P \cdot \sin 30^\circ \approx 19'620$$

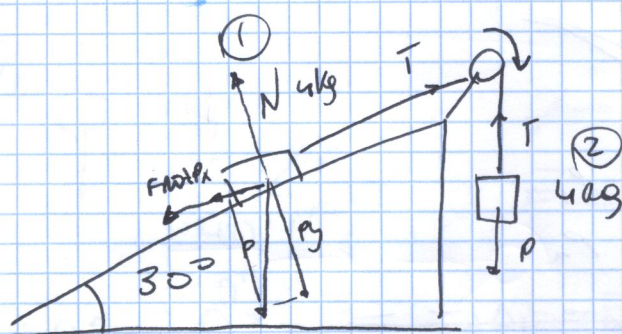
$$p_y = 33'98N = N$$

$$\left. \begin{aligned} (1) \quad \Sigma F &= T - F_{\text{not}} - P_x = 4 \cdot a \\ (2) \quad \Sigma F &= P - T = 4a \end{aligned} \right\}$$

~~$$- \text{Flot} - p_x + p = 89$$~~
~~$$- 19.62 + 19.62 = 89$$~~

36

$$T - F_{\text{roz}} - P_x = P - T$$



$$\text{Für die } \sum F_1 = \sum F_2$$

$$\mu = ?$$

$$\textcircled{1} P = 39'24 \text{ N}$$

$$P_x = 39'24 \cdot \sin 30 = 19'62$$

$$P_y = 33'98 \text{ N} = N$$

$$\textcircled{1} T - P_x - F_{\text{roz}} = m \cdot a$$

$$\textcircled{2} P - T = m \cdot a$$

$$\textcircled{2} P = 39'24 \text{ N}$$

$$\textcircled{42} \text{ in } T - P_x - F_{\text{roz}} = P - T;$$

$$T - 19'62 - F_{\text{roz}} = 39'24 - T$$

$$2T - 58'86 - F_{\text{roz}} = 0;$$

$$F_{\text{roz}} = 137'34 = \mu \cdot N;$$

$$\mu \cdot 33'98 = 137'34; \mu = -4'4 \text{ What}$$

Impulse

$$P = m \cdot v$$

$$\bar{F} = m \cdot a = \frac{m \cdot \bar{v}}{t} = \frac{\bar{P}}{t}$$

(1)

$$30 \text{ N s} = 2 \cdot \bar{v}$$

$$\bar{v} = 15 \text{ m/s}$$

(2)

$$30\vec{i} - 40\vec{j} \text{ } P_1$$

$$-30\vec{i} - 20\vec{j} \text{ } P_2$$

$$30\vec{i} - 40\vec{j} + x\vec{i} + y\vec{j} = -30\vec{i} - 20\vec{j}$$

$$\Delta p = F \cdot t$$

$$(-30\vec{i} - 20\vec{j}) - (30\vec{i} - 40\vec{j}) = F \cdot 4$$

$$-60\vec{i} + 20\vec{j} = F \cdot 4$$

$$F = -15\vec{i} + 5\vec{j}$$

(3)

$$50 \text{ s} = 0.05 \text{ kg}$$

$$3 \text{ m/s}$$

$$0.2 \text{ s}$$

$$-5 \text{ m/s}$$

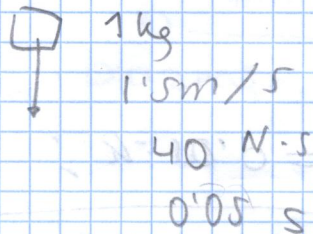
$$|F| = \left| \frac{m \cdot \Delta v}{\Delta t} \right| = \left| \frac{0.05 \cdot (-8)}{0.2} \right| = |-2 \text{ N}| = 2 \text{ N}$$

$$\Sigma F = m \cdot a$$

$$\vec{p} = m \cdot \vec{v}$$

$$\vec{F} \cdot t = m \cdot \vec{v}$$

(4)



$$\vec{F} = \frac{m \cdot \Delta \vec{v}}{\Delta t}$$

$$\Delta t \cdot \vec{F} = m \cdot \Delta \vec{v}$$

$$\Delta \vec{v} = \frac{0.05 \cdot 40}{1}$$

$$\Delta \vec{v} = 2$$

$$v_2 - v_1 = 2$$

$$v_2 - (-1.5) = 2$$

$$v_2 = 0.5 \text{ m/s}$$

(5) $\vec{p} = 5\vec{i} + 20\vec{j}$

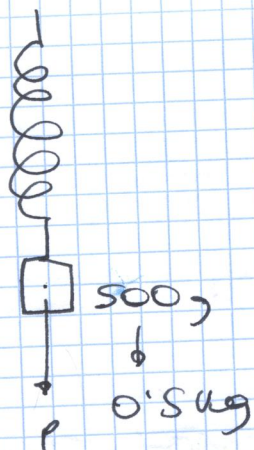
$$\Delta \vec{p} = \frac{\Delta \vec{p}}{t}$$

$$-10\vec{i} + 5\vec{j} = \frac{\vec{p}_F - (5\vec{i} + 20\vec{j})}{3}$$

$$-30\vec{i} + 15\vec{j} = \vec{p}_F - (5\vec{i} + 20\vec{j})$$

$$\begin{aligned} \vec{p}_F &= (-30\vec{i} + 15\vec{j}) + (5\vec{i} + 20\vec{j}) \\ &= -25\vec{i} + 35\vec{j} \end{aligned}$$

32



$$x = 5 \text{ cm} = 0.05 \text{ m}$$
$$K = ?$$

$$F = x \cdot K;$$

$$F = P \cdot g = 4.9 \text{ N};$$

$$4.9 \text{ N} = 0.05 \cdot K;$$

$$K = -98 \text{ N/m}$$

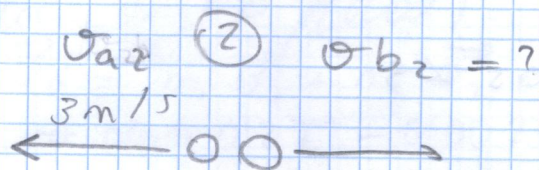
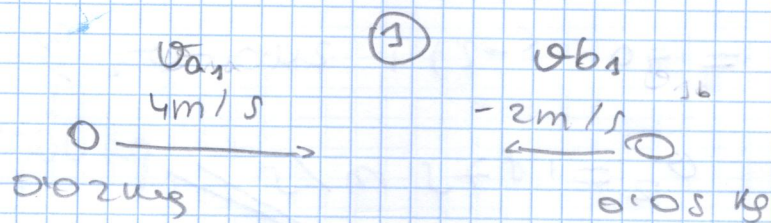
es negativo porque
opone al movimiento.

trata de devolver
el muelle a su
estado natural
lo.



conservación momento lineal

20g 0.02 kg
80g 0.05 kg



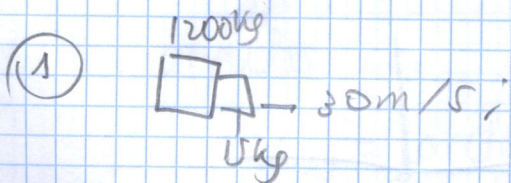
$$\left(\vec{P}_{\text{inicial}} \right)_{\text{total}} = \left(\vec{P}_{\text{final}} \right)_{\text{total}}$$

$$m_1 \cdot v_{a1} + m_{b1} \cdot v_{b1} = m \cdot v_{a2} + m \cdot v_{b2}$$

$$0.02 \cdot 4 + 0.05 \cdot (-2) = 0.02 \cdot (-3) + 0.05 \cdot v_{b2}$$

$$-0.02 = -0.06 + 0.05 v_{b2}$$

$$\frac{0.04}{0.05} = v_{b2} = 0.8 \text{ m/s} //$$



$$\vec{P} = m \cdot \vec{v}$$

$$P_{\text{inicial}} = 15 \cdot 30$$

$$P_{\text{final}} = 1200 \cdot v_2$$

$$v_2 = 0.375 //$$

②

$$P_i = P_f$$

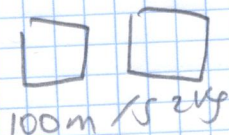
$$340 \cdot 1 = 70 \cdot (-2) + 240 \cdot v_2 ;$$

$$v_2 = 1.575 \text{ m/s} //$$



③

$$30g = 0.03 \text{ kg}$$



$$(\vec{P}_{\text{initial total}}) = (\vec{P}_{\text{final total}}) ;$$

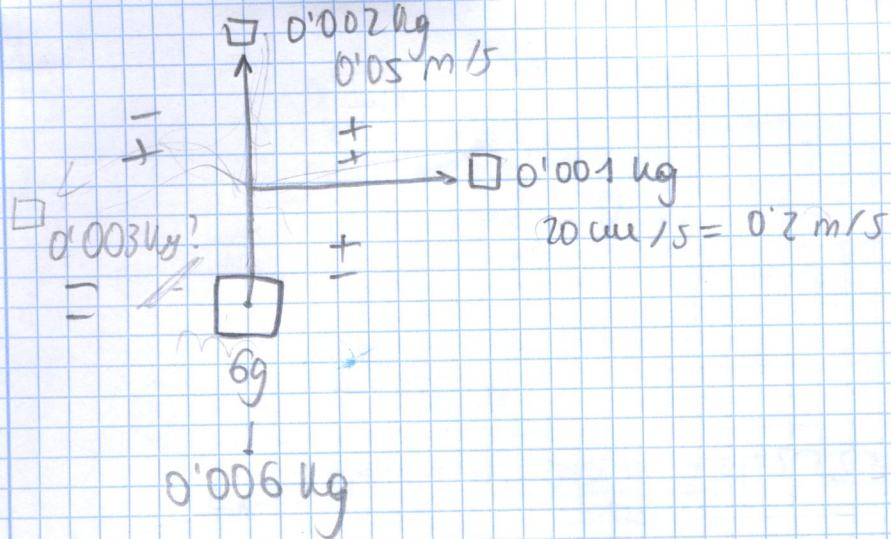


$$0.03 \cdot 100 = 2.003 \cdot v_2$$

$$1.5 \text{ m/s} //$$

④





$$\frac{\text{cm}}{s} \cdot \frac{1 \text{ m}}{100 \text{ cm}}$$

$$(\vec{p}_{\text{inicial}}) \equiv (\vec{p}_{\text{final}})$$

$$m_0 \cdot \vec{v}_0 = m_1 \cdot \vec{v}_1 + m_2 \cdot \vec{v}_2 + m_3 \cdot \vec{v}_3$$

$$0.006 \cdot 0 = 0.001 \cdot 0.2 \vec{i} + 0.002 \cdot 0.05 \vec{j} + 0.003 \cdot \vec{v}_3$$

$$0 = \frac{-2 \cdot 10^{-4}}{0.003} - \frac{1 \cdot 10^{-4}}{0.003} = \vec{v}_3$$

$$\vec{v}_3 = -0.0666 \vec{i} - 0.0333 \vec{j}$$

$$|\vec{v}_3| = \sqrt{(0.066)^2 + (0.033)^2} = \sqrt{5.53 \cdot 10^{-3}}$$

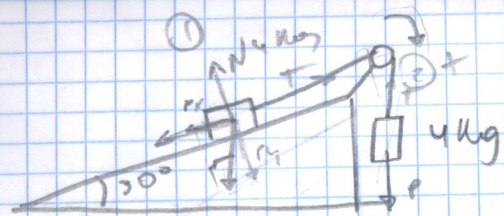
$$= 5.53 \text{ cm/s} \quad 0.074 \text{ m/s} = 7.4 \text{ cm/s}$$

ângulo:

$$\alpha_{v_3} = \arctg \frac{0.0333}{0.0666} = 26^\circ 33' 54.1''$$

em 3º e 4º quadrante:

$$206^\circ 33' 54.1''$$



$$\sum F_1 = \sum F_2$$

$$\mu = 1$$

$$\textcircled{1} P = 49.05 \text{ N}$$

$$P_x = 49.05 \cdot \sin 30 = 24.525 \text{ N}$$

$$P_y = 49.05 \cdot \cos 30 = 42.78 \text{ N}$$

$$\downarrow T - P = 0 \quad T = P$$

$$\sum F = P - T = 0$$

$$\textcircled{1} \sum F = T - P_x - F_{\text{frict}} = 0;$$

$$T - 24.525 - F_{\text{frict}} = 0;$$

$$T = 24.525 + F_{\text{frict}}$$

$$T - P_x - F_{\text{frict}} = 0$$

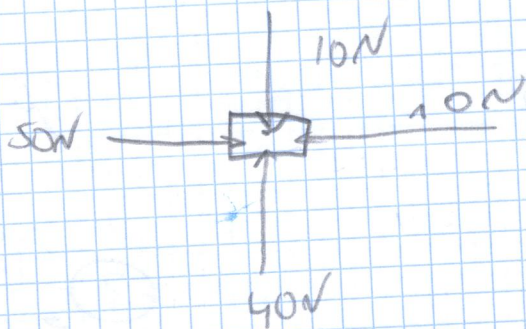
$\textcircled{2}$

$$\sum F = P - T = P - (24.525 + F_{\text{frict}}) = 0$$

$$49.05 - 24.525 - F_{\text{frict}} = 0;$$

$$F_{\text{frict}} = 24.525 \text{ N} = \mu \cdot 42.78;$$

$$\mu = \frac{24.525}{42.78} = 0.57 \text{ N}\cdot\text{s}$$



~~$$\Sigma F = (50 - 10) + (40 - 10) =$$~~

~~$$\Sigma F = 0;$$~~

~~$$F + 50 - 10 + 40 - 10 = 0;$$~~

~~$$F$$~~

$$F = m \cdot g = G \cdot \frac{m \cdot M}{d^2}$$

$$F = k \cdot \frac{q_1 \cdot q_2}{d^2}$$

$$100 \text{ N} = 6.67 \cdot 10^{-11} \cdot \frac{10^{10} \cdot 10^{15}}{d^2}$$

(después)

$$20N \rightarrow \text{lf } 25\text{cm} = 0.25\text{m}$$

$$30N \rightarrow \text{lf } 30\text{cm} = 0.30\text{m}$$

$$F = x \cdot k$$

$$20 = k \cdot (l - l_0)$$

$$\left. \begin{aligned} 20 &= k \cdot (0.25 - l_0) \\ 30 &= k \cdot (0.3 - l_0) \end{aligned} \right\}$$

~~$$20 = k \cdot (l - l_0)$$~~

~~$$20 = k \cdot (l - l_0)$$~~

$$\left. \begin{aligned} 20 &= k \cdot (0.25 - l_0) \\ 30 &= k \cdot (0.3 - l_0) \end{aligned} \right\}$$

$$k = \frac{20}{0.25 - l_0}$$

$$30 = \frac{6 - 20l_0}{0.25 - l_0}$$

$$7.5 - 30l_0 = 6 - 20l_0$$

$$1.5 = 10l_0$$

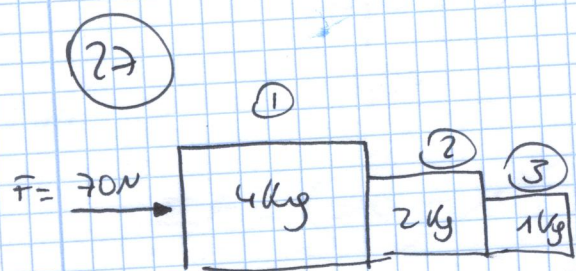
$$l_0 = 0.15\text{m} = 15\text{cm}$$

$$\begin{array}{r} 20 \\ 0.3 \\ \hline 60 \\ 0.5 \end{array}$$

$$\begin{array}{r} 0.25 \\ 30 \\ \hline 7.5 \end{array}$$

$$F = m \cdot a = \frac{m \cdot \Delta v}{\Delta t} = \frac{\Delta p}{\Delta t};$$

$$I = F \cdot \Delta t \quad N \cdot s$$



a sistema?

$$\Sigma F = m \cdot a;$$

$$\left. \begin{array}{l} 1) \{ \Sigma F_1 = 70N - F_{12} = m_1 \cdot a \\ 2) \{ \Sigma F_2 = F_{12} - F_{23} = m_2 \cdot a \\ 3) \{ \Sigma F_3 = F_{23} = m_3 \cdot a \end{array} \right\}$$

$$2) \Sigma F_2 = F_{12} - (m_3 a) = m_2 a;$$

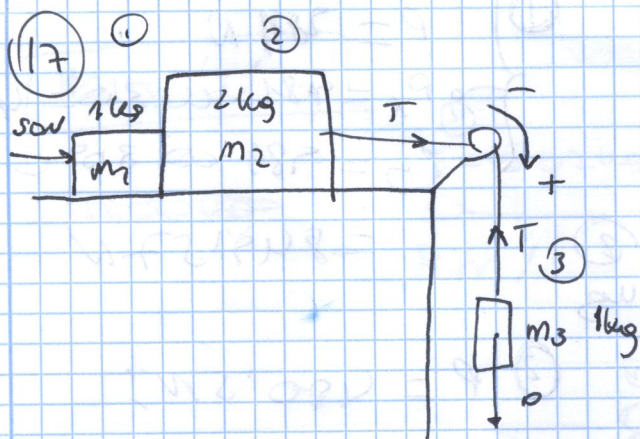
$$F_{12} - a = 2a;$$

$$F_{12} = 3a;$$

$$1) 70N - 3a = 4a;$$

$$70N = 7a;$$

$$a = 10 \text{ m/s}^2$$



plano inclinado
 dosques
 poleas
 cuerda
 campo eléctrico
 muelle

carpo 1 y 2

~~3/7 m~~

$$\left. \begin{array}{l} 1) \text{ } SON - F_{12} = m \cdot a \\ 2) \text{ } T - F_{12} = m \cdot a \\ 3) \text{ } 9'81 - T = m \cdot a \end{array} \right\} \left\{ \begin{array}{l} SON - F_{12} = a \\ T - F_{12} = 2a \\ 9'81 - T = a \end{array} \right. \left. \begin{array}{l} T = 2a + F_{12} \\ -T = a - 9'81 \\ T = 9'81 - a \end{array} \right\}$$

~~$$\begin{aligned} SON - F_{12} &= 9'81 - T \\ SON - F_{12} &= 9'81 - 2a - F_{12} \\ SON - 9'81 &= a \\ \hline 2a &= \end{aligned}$$~~

$$T - F_{12} = 2a;$$

$$9'81 - a - F_{12} = 2a;$$

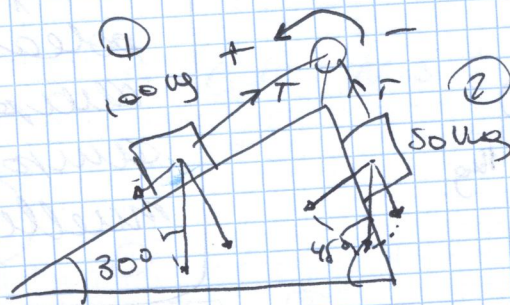
$$-F_{12} = 2a + a - 9'81;$$

$$F_{12} = 3a - 9'81;$$

$$50 - 3a + 9'81 = a;$$

$$59'81 = 4a;$$

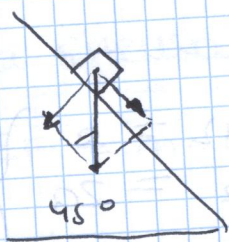
$$a = 14'9525 \text{ m/s}^2$$



$$\begin{aligned} P &= 981 \text{ N} \\ P_x &= 981 \cdot \cos 30^\circ = 849.57 \text{ N} \\ P_y &= 981 \cdot \sin 30^\circ = 490.5 \text{ N} \end{aligned}$$

$$\textcircled{2} P = 490.5 \text{ N};$$

$$\begin{aligned} P_x &= 490.5 \cdot \cos 45^\circ = 346.8 \text{ N} \\ P_y &= 490.5 \cdot \sin 45^\circ = 346.8 \text{ N} \end{aligned}$$



Al tercer cuerpo P_x el cuerpo 1,
está hacia la izquierda

$$\Sigma F = m \cdot a$$

$$\Sigma F_1 = P_x - T = m \cdot a;$$

$$\rightarrow 490.5 - T = 100a$$

$$\Sigma F_2 = T - P_x = m \cdot a;$$

$$\rightarrow T - 346.8 = 50a$$

$$\begin{aligned} -T + 490.5 &= 100a \\ T - 346.8 &= 50a \end{aligned}$$

$$143.66 = 150a;$$

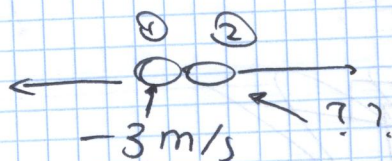
$$a = 0.96 \text{ m/s}^2$$

Resuelto 3

~~1200 kg~~

①
 $20g = 0.02kg$
 $\rightarrow 4m/s$

②
 $50g = 0.05kg$
 $\leftarrow 2m/s$



$$\left(\vec{p}_{total\ initial} \right) = \left(\vec{p}_{total\ final} \right) \quad \vec{p} = m \cdot \vec{v}$$

$$m_1 \cdot v_1 + m_2 \cdot v_2 = m_1 \cdot v_1' + m_2 \cdot v_2'$$

$$0.02 \cdot 4 + 0.05 \cdot (-2) = 0.02 \cdot (-3) + 0.05 \cdot v_2'$$

$$-0.02 = -0.06 + 0.05 v_2'$$

$$\frac{0.04}{0.05} = v_2' = 0.8 m/s //$$